## CAMBRIDGE INTERNATIONAL EXAMINATIONS Cambridge International General Certificate of Secondary Education

## MARK SCHEME for the March 2016 series

## 0580 MATHEMATICS

0580/42

Paper 4 (Extended), maximum raw mark 130

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PMT

## Abbreviations

cao	correct answer only
dep	dependent
FT	follow through after error
isw	ignore subsequent working
oe	or equivalent
SC	Special Case
nfww	not from wrong working
	not nom wrong working

soi seen or implied

	Qu.	Answers	Mark	Part Marks
1	(a)	$\frac{8}{8+15+9} \times 640$ oe	1	With no errors seen
	(b)	300 and 180	2	B1 for each or SC1 for answers reversed
	(c)	10 nfww	2	<b>M1</b> for 160 ÷ 15.25 implied by 10.5 or 10.49 nfww
	(d)	$\frac{7}{24}$	3	<b>M1</b> for $\frac{3}{8} + \frac{1}{3}$ oe
				<b>M1dep</b> on previous <b>M1</b> for $1 - their(\frac{3}{8} + \frac{1}{3})$ oe
2	(a)	Correct perpendicular bisector of <i>AB</i> with 2 pairs of correct arcs isw	2	<b>B1</b> for accurate with no/wrong arcs or <b>M1</b> for correct intersecting arcs with no or wrong line
	(b)	Correct angle bisector at A with two pairs of correct arcs isw	2	<b>B1</b> for accurate with no/wrong arcs or <b>M1</b> for two pairs of correct arcs with no or wrong line
	(c)	Circle centre $E$ radius 5 cm isw	2FT	<b>FT</b> circle centre <i>their E</i> radius 5 cm provided (a) and (b) attempted
				<b>M1</b> for $250 \div 50$ oe soi e.g. from arc If 0 scored <b>SC1</b> for circle centre <i>their E</i>
	(d)	R	2	сао
		R		B1 for each If 0 scored, SC1 for two 'correct' regions but in part (c), centre correct but radius incorrect

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	Qu.	Answers	Mark	Par	t Marks	
3	(a) (i)		3	B1 for each		
5	(4) (1)		5			
	(ii)	46	1FT	<b>FT</b> 29 + <i>their</i> 3 values	s from (a)	
	(iii)	11	1			
	(iv)	$\frac{7}{19}$ oe	2	<b>M1</b> for $\frac{n}{16 + their3}$ (9)	0 < n < (16 −	- their 3))
	(b) (i) (ii)	$\frac{9}{200}$ or 0.045	1 3	or $\frac{4 + their 3}{k}$ (k > (4 - M2 for $\frac{1}{2}$ (900 + 1500		
	(iii)	7.2	1FT	or <b>M1</b> for method of f <b>FT</b> ( <i>their</i> 10800) ÷ 15	inding a rele	vant area
4		64	1	<b>FI</b> ( <i>inetr</i> $10800$ ) ÷ 13	000	
4	(a) (i) (ii)	16 to 16.5	2	<b>M1</b> for UQ = 71 to 71	$5 \text{ or } I \Omega = 55$	
	(ii) (iii)	62	2	<b>B1</b> for 24 indicated	of EQ –5.	,
	(iv)	6	2	<b>B1</b> for 54 seen		
	(b)	[8] 12 23 11 [4] 2	3	<b>B2</b> for 1 incorrect read	ding FT othe	S
	(c)	Blocks of height 0.6 2.3 1.1 0.4 with correct widths	4FT	<ul> <li>B1 for 2 correct</li> <li>FT <i>their</i> (b) for heigh</li> <li>B1FT for each correc</li> <li>If B0, SC1 for blocks or for <i>their</i> correct free</li> </ul>	ts t block of widths 20	, 10, 10, 10
5	(a)	6250	3	<b>M2</b> for $\frac{6000}{100-4} \times 100$ or <b>M1</b> for 6000 assoc		
	(b)	4441	3	<b>B2</b> for 4441.1 to 4441 or <b>M1</b> for $\frac{6000}{1.351}$		. [ \ A]

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	Qu.	Answers	Mark	Part Marks
	(c)	1.58 or 1.581	5	<b>M1</b> for $6000 \times \left(1 + \frac{1.5}{100}\right)^8$ oe
				A1 for 6758.95 or 6758.96 to 3 sf or better or 758.95 or 758.96 rounded or truncated to 3 sf
				and M2 for
				${their(6000 \times 1.015^8) - 6000} \times \frac{100}{6000 \times 8}$ oe
				or <b>M1</b> for $\frac{6000 \times r \times 8}{100}$ oe
6	(a) (i)	Rotation	1	
		90° [anticlockwise] oe	1	
		(4,4)	1	
	(ii)	Enlargement	1	
		[centre] (5,1)	1	
		[scale factor] 2	1	
	(b) (i)	Image at $(-2, 5) (-2, 7) (-1, 7)$	2	<b>B1</b> for translation by $\begin{pmatrix} -5\\k \end{pmatrix}$ or $\begin{pmatrix} k\\3 \end{pmatrix}$
	(ii)	Image at $(-2, 1) (-2, -1) (-1, -1)$	2FT	<b>FT</b> <i>their</i> triangle <i>P</i> reflected in line $y = 3$ <b>B1</b> for reflection of <b>triangle</b> <i>P</i> in the line $x = 3$ or $y = k$
	(c)	Image at (-2, 3) (-4, 3) (-4, 4)	3	<b>B2</b> for 2 vertices correct in triangle or 3 correct co-ordinates soi in working or <b>B1</b> for 1 vertex in triangle correct soi
				or <b>M1</b> for $\begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix} \begin{pmatrix} 3 & 3 & 4 \\ 2 & 4 & 4 \end{pmatrix}$ shown
				or statement rotation 90° [ anticlockwise] about (0, 0)
7	(a)	3.5[0] 1.94 3.11	3	B1 for each
	(b)	Fully correct curve	5	<b>B3 FT</b> for 10 or 11 points or <b>B2 FT</b> for 8 or 9 points or <b>B1 FT</b> for 6 or 7 points
				<b>B1 indep</b> two separate branches not touching or cutting <i>y</i> -axis
				SC4 for correct curve, but branches joined
	(c)	-0.7 to $-0.6$	1	

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Qu.	Answers Mark H		Par	rt Marks	
(d) (i)	-1 2.5	1 1	If 0,0, <b>M1</b> for $y = 2.5$	-x oe seen i	n working
(ii)	-0.6 to $-0.5$ with correct ruled line	3	<b>B2FT</b> for drawing <i>the</i> or <b>M1</b> for ruled line the gradient -1 FT		
(e)	Correct tangent and $0.5 \leq \text{grad} \leq 0.85$	3	<b>B2</b> for close attempt a answer in range OR <b>B1</b> for ruled tangent a $x = 2$ Consider point of con two vertices of daylig between $x = 1.8$ and 2	t $x = 2$ , no da tact as midpo ht, the midpo	ylight at int between
			and M1 (dep on B1 o [at any point] for $\frac{ris}{ru}$	se	pt at tangent
(a)	15 nfww	3	<b>M1</b> for $y = k\sqrt{x+2}$	2) oe	
(b)	$\frac{x+6}{x-2}$ nfww final answer	5	A1 for $k = 3$ B2 for $(x+6)^2$ oe or SC1 for $(x+a)(x+a)(x+b) = 12$ or $x(x+6)$	,	<i>b</i> = 36 or
(c)	$\frac{X}{W^2+1}$ nfww final answer	5	<b>B2</b> for $(x-2)(x+6)$ or <b>SC1</b> for $(x+a)(x+6) = 0$ or $x(x-2) + 6(x-2)$ <b>M1</b> for $W^2 = \frac{X-a}{a}$ <b>M1</b> for next production	(+b) where $a- 2(x + 6)or W\sqrt{a} = \sqrt{2}$	
			M1 for 2nd productiv M1 for 3rd productive M1 for final step lead	e step	
(d)	$\frac{-7x-1}{x^2-1} \text{ or } \frac{-7x-1}{(x-1)(x+1)}$ final answer	5	M1 for common denoted M1 for $(x-2)(x-1)$		

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	Qu.	Answers	Mark	Part Marks
9	(a) (i)	У	1	
	(ii)	$\mathbf{x} + \mathbf{y}$	1	
	(iii)	$\mathbf{x} + 2\mathbf{y}$	2	M1 for a correct unsimplified route or identifying $\overrightarrow{OS}$
	(b)	$-(\frac{1}{2}\mathbf{x}+\mathbf{y})$ oe	2	M1 for a correct unsimplified route or $\overrightarrow{GR} = -\frac{1}{2} \mathbf{x}$ or $\overrightarrow{RG} = \frac{1}{2} \mathbf{x}$
	(c) (i)	$\overrightarrow{MG} = 2\mathbf{x} + 2\mathbf{y}$	2	<b>M1</b> for a correct unsimplified route e.g. $2 \overrightarrow{PQ}$
	(ii)	$\overrightarrow{MH} = \mathbf{x} + \mathbf{y} \text{ or } \overrightarrow{HG} = \mathbf{x} + \mathbf{y}$	M1	Accept $\overrightarrow{HM} = -\mathbf{x} - \mathbf{y}$ or $\overrightarrow{GH} = -\mathbf{x} - \mathbf{y}$
		$\overrightarrow{MG} = 2\overrightarrow{MH}$ oe	A1	Dep on (c)(i) correct, arrows essential
10	(a)	5.2[0] or 5.196	3	<b>M2</b> for $[h^2=] 6^2 - 3^2$ or better
				or <b>M1</b> for $h^2 + 3^2 = 6^2$ or <b>B1</b> for <i>PR</i> (or <i>PQ</i> or <i>QR</i> ) = 6
	(b) (i)	7.2[0] or 7.196	1FT	<b>FT</b> their (a) $+ 2$
	(ii)	62.4 or 62.35	5	<b>M4</b> for $12 \times 6 \times \frac{1}{2}$ tan 60 oe
				or <b>M3</b> for $6 \times \frac{1}{2}$ tan 60 oe
				or M2 for realising that $\frac{1}{2}$ base = 1 × tan60 oe
				or <b>B1</b> for angle 30 or 60 in correct position on diagram or in a calculation
				If <b>0</b> scored, <b>SC1</b> for volume = an area $\times$ 12 seen
11	(a) (i)	11	1	
	(ii)	14x + 3 final answer	1	
	(b)	17 - 21x final answer	2	<b>M1</b> for $7(2-3x) + 3$ oe
	(c)	$-\frac{1}{2}$	3	<b>M1</b> for $3(2-3x) = 7$ oe
		9		M1 for correct first step
	(d)	-1.3	3	<b>M1</b> for $2-3(x+4)-(7x+3)=0$
				M1 for $-10x - 13 = 0$ oe
				If <b>0</b> scored, <b>SC1</b> for answer $-0.7$ oe after $2-3(x+4)-7x+3=0$ shown previously